# Simulating CSMA/CA Behavior for Performance Evaluation of Multi-hop Wireless Networks 

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#### Abstract

In this paper, we design an efficient method of simulating wireless networks that use CSMA/CA-based protocols in the MAC layer. In the method, a stochastic model to estimate the CSMA/CA frame transmission delay is naturally incorporated into the conventional fully event-based model. The stochastic model can simplify the interactions between a frame transmitter and its surrounding nodes, which alleviates the event scheduling overhead in simulation. The important feature is that the stochastic model can be applied in "per-node" and "time" basis, i.e. we may simulate the behavior of some intended nodes precisely while the others are simplified by the stochastic mode to save computational resources. To the best of our knowledge, this is the first approach to coexistence of the stochastic and eventbased models in wireless multi-hop network simulation. We have implemented this scheme in a commercial network simulator and conducted several experiments. From the results, it is confirmed that the proposed method could perform simulation of frame transmission much faster than the fully event-based simulation achieving the same accuracy as the conventional model.


Index Terms-Wireless Network Simulation, CSMA/CA

## I. Introduction

Wireless networks including most-popular IEEE802.11based networks are deployed everywhere nowadays. In order to assess the behavior of those networks and evaluate their performance, field experiments, mathematical analysis and network simulations are usually conducted depending on the network size and evaluation purposes. Network simulators are often required to be efficient in terms of memory space and processing power because they should usually deal with largescale networks such as vehicular ad-hoc networks and wireless sensor networks, or they should be run a number of times for exhaustive tests of applications. In particular, it is known that event scheduling in the MAC-layer frame transmission consumes a lot of computational resources in wireless network simulations [1], [2]. Accordingly, several techniques have been proposed to deal with this issue [3], [4], [5], [6].

In this paper, we design an efficient method of simulating wireless networks that use CSMA/CA-based protocols in the MAC layer. In the method, a stochastic model to estimate the CSMA/CA frame transmission delay is naturally incorporated into the conventional fully event-based model. The idea is that the channel acquisition before a frame transmission sequence in CSMA/CA, which needs scheduling/rescheduling many events to many nodes, is modeled as a probabilistic duration that can be computed simply. Since this abstraction is done within the event-driven simulation scheme, the stochastic model can adaptively be applied in "per-node" and "time"
basis. In other words, the abstract level of simulation can be adapted spatially and temporally, depending on upper-layer applications such as routing and video streaming. We have implemented this scheme in a commercial network simulator called Scenargie [7] and conducted several experiments. From the results, the proposed method could perform simulation of frame transmission faster than the "pure" event-based simulation

## II. Fully Event-based Modeling of CSMA/CA

The significant feature of IEEE 802.11 DCF is the back-off mechanism to avoid collision. When a node wishes to send a MAC frame, the node has to listen to the channel during a random back-off time before sending the frame. The back-off is suspended during its neighboring nodes' transmission.
The fully event-based model simulates these operations by scheduling three events, "back-off timer", "send-begin" and "send-end". Let us assume that node A and node B try to send frames to node C in Fig. 1. These nodes schedule "backoff timer" events with random delay. In this figure, node B can send the frame earlier than node A because node A has a longer back-off time value and the "back-off timer" event of node B is executed first. Node B schedules "send-begin" events and "send-end" events to its neighbor nodes A and C immediately after its "back-off timer" event, in order to notify its transmission. Meanwhile, node A re-schedules its "backoff timer" event to wait for the channel to be idle as the node receives "send-begin" and "send-end" events.

The fully event-based model can also represent frame reception by those "send-begin" and "send-end" events. Fig. 2 shows an example that node C receives frames from node A and node B. Let us assume the following situation. Firstly, nodes A and B cannot listen to each other's transmission (i.e. they are hidden terminals of each other). Node A schedules "send-begin" and "send-end" events to its neighbor nodes. Node C knows that node A sends a frame to node C by these events, examines whether the radio signal strength is sufficient to receive the frame or not, and finally determines that the frame cannot be received due to weak signal strength (this information is obtained from the physical layer simulation). Then node B begins to send a frame and node $C$ cannot receive it due to interference at node C by the signal from node A (hidden terminal interference). As such, if node C receives the "send-begin" event, it needs to check whether or not there are other "send-begin" events scheduled before the "send-end" event to know the possibility of data frame collision.


Fig. 2. Receiving a frame
In this way, the fully event-based model can exactly simulate the complete interactions of CSMA/CA, but it is necessary to schedule/reschedule a lot of events. Therefore, large-scale network simulation requires a lot of computing resources.

## III. Stochastic event-driven model of CSMA/CA

In our proposed model, each node that wishes to transmit a frame never utilizes the original back-off process. Instead, it computes the estimated delay to acquire the channel, which is called channel acquisition delay hereafter. This computation is done online knowing the surroundings' recent traffic status, i.e., the traffic amount transmitted by its neighbors as well as its own traffic amount to be transmitted. Based on the information, the probability function is designed for this estimation purpose. Following the probability, the channel acquisition process of CSMA/CA is simplified keeping very similar packet loss ratio with the original CSMA/CA process. In this way, the proposed model can simulate each frame transmission independently without confirming other frame transmissions. Therefore, when a node sends a frame, the proposed model schedules "send-begin" event and "send-end" event for only its receiver node to which the frame is delivered. It is not necessary to schedule any events for other neighbor nodes. This can contribute to the reduction of simulation costs. Although this basic idea is based on a technique to analyze IEEE 802.11 DCF [8], the other parts of the original mechanism such as the retransmission mechanism are kept intact for accuracy of simulation. As stated above, our goal is to reduce the number of events to be scheduled and/or rescheduled due to back-off interruption.

Basically, this model is based on the stochastic model proposed in Ref. [8] and modified to derive channel acquisition delay for the event-based simulation. In the method, we use two probabilities $S_{n}^{\prime}\left(t^{\prime}\right)$ and $L_{n}$ to model the operation of

IEEE 801.11 DCF. We let $N_{n}$ denote a set of node $n$ and its neighbors. $S_{n}^{\prime}\left(t^{\prime}\right)$ is a probability that at least one node of $N_{n}$ sends frames in idle time slot $t^{\prime} . L_{n}$ is a probability that a frame received by node $n$ collides. The symbols $S$ and $L$ respectively come from "Sending of frames" and "Loss of frames", and symbols with prime mean that those symbols are defined with respect to idle time slots. We design $S_{n}^{\prime}\left(t^{\prime}\right)$ and $L_{n}$ in the following.

## A. Computation of Probabilities in Stochastic Event-driven Model

We denote as $h_{n}(t)$ the frame arrival ratio from the network layer in time slot $t$ of node $n$. This is given as an input and we assume it follows $\sum_{t=0}^{\infty} h_{n}(t)=1$. Let us denote an average transmission time as $T_{n}$, which is duration from transmission of RTS till reception of ACK or ACK timeout. We also denote the probability that at least one node of $N_{n}$ sends a frame in time slot $t$ as $S_{n}(t)$. By using these variables, we can derive the probability denoted by $g_{n}(t)$ that node $n$ begins to process back-off at time slot $t$ as follows.
$g_{n}(t)=\left(\prod_{x=t-T_{n}+1}^{t}\left(1-S_{n}(x)\right)\right) \cdot h_{n}(t)+S_{n}\left(t-T_{n}\right) \cdot \sum_{x=t-T_{n}}^{t-1} h_{n}(x)$
The first part of this equation means the probability that node $n$ can begin its back-off process immediately after the node receives a frame from the network layer.The node can enter the back-off status without waiting because no neighbor node sends a frame in time slot $t$ and a wireless channel is idle. Meanwhile, if one of the neighbor nodes send a frame, the node $n$ cannot begin its back-off process immediately, and has to delay the transmission. The second part of this equation means that frames from the network layer between $t-T_{n}$ and $t-1$ time slots are scheduled to process at time slot $t$ because one of neighbor nodes has sent a frame at time slot $t-T_{n}$. We note that $\sum h_{n}(t)$ indicates the probability of receiving at least one frame from the network layer before $t$.

A frame collision may occur when two or more nodes send frames at the same time slot. In order to estimate how often the frame collision occurs, we focus on idle time slots that are not occupied by frame transmission. Let us recall that a "prime symbol" represents probabilities that only focus on idle time slots (i.e. busy slots are ignored). Let us assume $k$ frames have been sent by time slot $t$. This means that $k \cdot T_{n}$ time slots have been occupied and the last idle time slot $t^{\prime}$ is $t-k \cdot T_{n}$. Therefore, we can derive $g_{n}^{\prime}\left(t^{\prime}\right)$ from $g_{n}(t)$ and $C_{n}(t, k)$ by defining $t^{\prime} \triangleq t-k \cdot T_{n}$ where $g_{n}^{\prime}\left(t^{\prime}\right)$ is the probability that exactly $k$ frames have been sent by time slot $t$ among $N_{n}$.

$$
\begin{align*}
g_{n}^{\prime}\left(t^{\prime}\right) & =\sum_{k=0}^{\infty} C_{n}\left(t^{\prime}+k \cdot T_{n}, k\right) \cdot g_{n}\left(t^{\prime}+k \cdot T_{n}\right)  \tag{2}\\
C_{n}(t, k) & =C_{n}(t-1, k-1) \cdot S_{n}(t)+C_{n}(t-1, k) \cdot\left(1-S_{n}(t)\right)  \tag{3}\\
C_{n}(0, k) & =\left\{\begin{array}{cc}
1-S_{n}(0) & (k=0) \\
S_{n}(0) & (k=1) \\
0 & (k \geq 2)
\end{array}\right. \tag{4}
\end{align*}
$$

$C_{n}(t, k)$ consists of two parts: The first part represents that $k-1$ frames have been sent by time slot $t-1$ and a frame is sent at time slot $t$. The second part represents that $k$ frames have been sent by time slot $t-1$ and no frame is sent at time slot $t$.

Next, we will show how to calculate the probability denoted by $f_{n}^{\prime}\left(t^{\prime}\right)$ that node $n$ sends a frame at idle time slot $t^{\prime}$. If node $n$ sends a frame at idle time slot $t^{\prime}$, the node had begun a back-off process at certain idle time slot $x$ and had waited for $t^{\prime}-x$ idle time slots. Thus, $f_{n}^{\prime}\left(t^{\prime}\right)$ can be represented by two probabilities, $g_{n}^{\prime}\left(t^{\prime}\right)$ and $B\left(t^{\prime}-x, p c_{n}\right)$. The latter is the probability that node $n$ sends a frame after $t^{\prime}-x$ idle time slots, given the probability $p c_{n}$ of frame loss of node $n$.

$$
\begin{align*}
f_{n}^{\prime}\left(t^{\prime}\right) & =\sum_{x=0}^{t^{\prime}} g_{n}^{\prime}(x) \cdot B\left(t^{\prime}-x, p c_{n}\right)  \tag{5}\\
B\left(t^{\prime}-x, p c_{n}\right) & =\sum_{i=0}^{r}\left(p c_{n}\right)^{i} \cdot B_{i}\left(t^{\prime}-x\right) \tag{6}
\end{align*}
$$

$B\left(x, p c_{n}\right)$ represents the back-off process itself and is affected by frame retransmissions. It can be the sum of probability $B_{i}(x)$ that a node ends a back-off process of the $i$-th retransmission after $x$ idle time slots. $B_{i}(x)$ means that a node failed the $(i-1)$-th back-off process at certain time slot $y$ and the node begins the $i$-th back-off process with duration $x-y$.

Using $f_{n}^{\prime}\left(t^{\prime}\right)$, we can derive the probability $S_{n}^{\prime}\left(t^{\prime}\right)$ that at least one node in $N_{n}$ sends a frame at idle time slot $t^{\prime}$. Although this probability is used to simulate frame transmissions in the proposed model, we need frame loss probability $p c_{n}$ to calculate it and continue to process this formulation. We can also derive $S_{n}(t)$ using $S_{n}^{\prime}\left(t^{\prime}\right)$ and $C_{n}^{\prime}\left(t^{\prime}, k\right)$. $C_{n}^{\prime}\left(t^{\prime}, k\right)$ is the probability that exactly $k$ frames have been sent by idle time slot $t^{\prime}$.

$$
\begin{align*}
S_{n}^{\prime}\left(t^{\prime}\right) & =1-\prod_{n \in N_{n}}\left(1-f_{n}^{\prime}\left(t^{\prime}\right)\right)  \tag{7}\\
S_{n}(t) & =\sum_{k=0}^{\infty} C_{n}^{\prime}\left(t-k T_{n}, k\right) \cdot S_{n}^{\prime}\left(t-k T_{n}\right) \tag{8}
\end{align*}
$$

$C_{n}^{\prime}\left(t^{\prime}, k\right)$ is derived from $S_{n}^{\prime}\left(t^{\prime}\right)$ in the same manner as $C_{n}(t, k)$. If $k$ frames have been sent by idle time slot $t^{\prime}, t^{\prime}$ is time slot $t+k \cdot T_{n}$. Thus, $S_{n}^{\prime}\left(t^{\prime}\right)$ is equivalent to $S_{n}^{\prime}\left(t^{\prime}+k \cdot T_{n}\right)$ and we can derive (8) by defining $t \triangleq t^{\prime}+k \cdot T_{n}$.

Finally, we can derive the collision ratio in frame transmission. This is used to determine whether or not a node can receive a frame. We denote this probability as $L_{n}$.

$$
\begin{align*}
L_{n}^{\prime}\left(t^{\prime}\right) & =\frac{\sum_{i \in N_{n}} f_{i}^{\prime}\left(t^{\prime}\right)\left\{1-\prod_{j \neq i, j \in N_{n}}\left(1-f_{j}^{\prime}\left(t^{\prime}\right)\right)\right\}}{\sum_{i \in N_{n}} f_{i}^{\prime}\left(t^{\prime}\right)}  \tag{9}\\
L_{n} & =\lim _{t^{\prime} \rightarrow \infty} \frac{\sum_{x=0}^{t^{\prime}} L_{n}^{\prime}(x)}{t^{\prime}}  \tag{10}\\
p c_{n} & =\frac{\sum_{i \neq n, i \in N_{n}} L_{i}}{\left|N_{n}\right|-1} \tag{11}
\end{align*}
$$

$L_{n}^{\prime}\left(t^{\prime}\right)$ is the average length of transmission started at time slot $t^{\prime} . L_{n}^{\prime}\left(t^{\prime}\right)$ can be represented by their $f_{i}^{\prime}\left(t^{\prime}\right)$ since nodes in $N_{n}$ might send frames at the same time. In addition, using $L_{n}$, we obtain the probability $p c_{n}$ that a node fails to send a frame.

As shown in Eq.7, Eq. 10 and Eq.11, in order to calculate $S_{n}^{\prime}\left(t^{\prime}\right), L_{n}$ and $p c_{n}$ for node $n$, it is necessary to refer to $L_{i}$ and $f_{i}^{\prime}\left(t^{\prime}\right)$ where note $i$ is each neighbor node. Therefore, we must calculate the probabilities of all nodes at the same time so that we can simulate how the frame transmission of the nodes affects each other. The proposed method initially sets $S_{n}(t)=0$, and calculates the expressions repeatedly until $L_{n}$
converges. We can get $S_{n}^{\prime}\left(t^{\prime}\right)$ and $L_{n}$ of all nodes after that calculation.

## B. Modeling Frame Transmission

1) Sending a Frame: If node $n$ in the proposed model begins the back-off process at idle time $t^{\prime}$, the node first selects its back-off time randomly from its contention window size in the same way as the fully event-driven model. We denote this back-off time as $b$. Then using the expected number of frames sent, the total waiting time around node $n$, which is denoted as $B_{n}\left(t^{\prime}, b\right)$, is expressed as follows.

$$
\begin{align*}
B_{n}\left(t^{\prime}, b\right) & =b+T_{n} \cdot\left(M_{n}^{\prime}\left(t^{\prime}+b\right)-M_{n}^{\prime}\left(t^{\prime}\right)\right)  \tag{12}\\
M_{n}^{\prime}\left(t^{\prime}\right) & =\sum_{x=0}^{t^{\prime}} S_{n}^{\prime}(x) \tag{13}
\end{align*}
$$

$M^{\prime}\left(t^{\prime}\right)$ is the expected number of frames sent before idle time slot $t^{\prime}$, and consequently $M^{\prime}\left(t^{\prime}+b\right)-M^{\prime}\left(t^{\prime}\right)$ means the number of frames sent during the back-off process. After the total waiting time $B_{n}\left(t^{\prime}, b\right)$ elapses, the node sends "sendbegin" event and "send-end" events to the receiver node.
2) Receiving a Frame: In the proposed model, a node determines whether a frame can be received or not based on the probability calculated by Eq.(10). Concretely, when a node executes a "send-begin" event in order to receive a frame, the proposed model deferimine whether the node succeed to receive the frame or not. If so, the node continues to process the event and can receive the frame. If not, the node cancels the event.
3) Proposed and Fully Event-driven Models: By the proposed model, we can reduce the computational cost for simulations, but the simulation accuracy may not be perfect. To pursue the best trade-off between the computational cost and accuracy, we may apply the fully event-driven model to the set of nodes that need accurate simulations, and the proposed model to the rest of the nodes to reduce the number of events for speedup of simulations. In such case, the two models need several interactions to work properly. Basically, the nodes simulated by the fully event-driven model not only conduct conventional event-driven simulations but also calculate the above two probabilities like the nodes simulated by the proposed model. We will omit the details due to lack of space.

## IV. EXPERIMENTS

We have implemented the proposed mechanism in a commercial network simulator called Scenargie [7], and have conducted several experiments. In these experiments, we have measured both of the frame transmission delay (i.e. channel acquisition delay) and frame loss ratios in the MAC layer to evaluate the accuracy of simulations. We have also measured the number of scheduled "send-begin" events to observe the saving effect by our method.

Firstly, we have prepared a scenario where nodes can listen to each other (all the nodes are in the single hop range) and there are exactly one transmitter and one receiver. The transmitter sends a MAC frame in IEEE 802.11b to the receiver every 0.5 second. The frame size is 512 bytes. This scenario is designed to observe how a single frame transmission is scheduled in both models. Varying the number of neighbor

TABLE I
THE NUMBER OF SIMULATION EVENTS (WITH ONE TRANSMITTER)

| \# of <br> nodes | \# of events (Fully event-driven) |  | \# of events (Prpposed) |  |
| ---: | ---: | ---: | ---: | :---: |
|  | send-begin | all | send-begin | all |
| 10 | 47230 | 141696 | 4720 | 29500 |
| 20 | 94400 | 271399 | 4815 | 30165 |
| 30 | 141600 | 401199 | 4872 | 30564 |
| 40 | 188800 | 530998 | 4964 | 31208 |
| 50 | 236150 | 661255 | 5002 | 31474 |

nodes from 10 to 50 , we have measured the number of "sendbegin" events. Table I shows the number of "send-begin" and the number of all simulation events. The number of events in the traditional fully event-based model is proportional to the number of neighbor nodes, because the events were scheduled not only to the receiver node but also to the neighbor nodes in the fully event-based model. On the other hand, since the events were scheduled only to the receiver node in the proposed model, the number of the events in the proposed model was constant. We have also measured the frame loss ratios and frame transmission delay, and they were almost zero in both models. From these results, we can see that the proposed model can significantly reduce the number of the events, achieving the same simulation results.

Next, we have evaluated the affect of node density and behavior on the simulation performance and accuracy. We modified the previous scenario to let EVERY node except the receiver node transmit a MAC frame in IEEE 802.11b every 0.5 second and evaluated the same metrics. Table II shows the number of "send-begin" events and the number of all simulation events. From the result, we can see that the proposed model can reduce considerably the number of events especially when nodes are densely deployed. Fig. 3 shows the frame loss ratios in the MAC layer. In the proposed model, the frame loss ratio is directly determined by some probabilities, while it is adhere to the original CSMA/CA mechanism taking into consideration the physical layer effect in the fully eventbased model. In Fig. 3, we can observe that the calculated loss ratios are very close to those in the fully event-based model. Although a small gap between two lines has been observed, we have analyzed that this was due to probabilistic and unexpected behavior of the physical layer, which is almost impossible to perfectly follow for any abstraction technique that does not simulate radio propagation. The important feature here is that the two lines follow the same trend with at most $1 \%$ deviation. The same tread has been observed in frame transmission delay shown in Fig. 4. The maximum deviation was about less than 1 ms , which is negligible for many large-scale networks such as WSNs.

## V. Conclusion

In this paper, we have proposed a new stochastic model for simulating the MAC layer behavior. The proposed model determines whether a node can transmit MAC frames or not using probabilities to reduce the number of simulation events. We have implemented the proposed model in a commercial network simulator, and carried out several experiments. From the experimental results, the proposed model could reduce the number of events maintaining certain accuracy.

TABLE II
THE NUMBER OF SIMULATION EVENTS (WITH $n-1$ TRANSMITTER)

| \# of <br> nodes | \# of events (Fully event-driven) |  | \# of events (Prpposed) |  |
| ---: | ---: | ---: | ---: | ---: |
|  | Send-begin | all | send-begin | all |
| 10 | 472170 | 1423622 | 47200 | 295001 |
| 20 | 1919380 | 5527932 | 96049 | 601545 |
| 30 | 4384830 | 12402331 | 146278 | 917749 |
| 40 | 7919720 | 22148162 | 198336 | 1246756 |
| 50 | 12563150 | 34848197 | 251693 | 1584861 |



Fig. 3. Frame loss ratio ( $n-1$ transmitters)


Fig. 4. Frame transmission delay ( $n-1$ transmitters)

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